**Common Core State Standards** 

# Geometry

**Traditional Pathway** 



**Program Overview** 



This program was developed and reviewed by experienced math educators who have both academic and professional backgrounds in mathematics. This ensures: freedom from mathematical errors, grade level appropriateness, freedom from bias, and freedom from unnecessary language complexity.

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#### **Standards Correlations**

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Two-Dimensional Cross Sections of Three-Dimensional Objects

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GeoGebra. "Sections of Cubes."

GeoGebra. "Sections of Cylinders."

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GeoGebra. "Sections of Triangular Pyramids."

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GeoGebra. "Similar Circles?"

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#### **Standards Correlations**

#### **Unit Assessment**

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## Introduction

The *Common Core State Standards Traditional Pathway: Geometry Program* is a complete set of materials developed around the Common Core State Standards, the CCSS curriculum map in Appendix A, and the Geometry course descriptions. The components are designed to support students in meeting and exceeding the standards encompassed by the Geometry course. The program realizes the benefits of exploratory and investigative learning, and employs a variety of instructional models to meet the needs of students across the range of learning styles.

This program realizes the benefits of exploratory and investigative learning and employs a variety of instructional models to meet the learning needs of students with a range of abilities.

The *Common Core State Standards Traditional Pathway: Geometry Program* includes components that support problem-based learning, instruct and coach as needed, provide practice, and assess students' skills. Instructional tools and strategies are embedded throughout.

The set of unit materials or digital version of the program includes:

- More than 150 hours of lessons, addressing the six units of CCSS TP: Geometry
- Essential Questions for each instructional topic
- Vocabulary
- Instruction and Guided Practice
- Problem-based Tasks and Coaching questions
- Step-by-step graphing calculator instructions for the TI-Nspire and the TI-83/84
- Station activities to promote collaborative learning and problem-solving skills

#### **Purpose of Materials**

The *Common Core State Standards Traditional Pathway: Geometry Program* has been organized to coordinate with the CCSS Traditional Pathway: Geometry content map and specifications from Appendix A of the Common Core State Standards.

Each lesson includes activities that offer opportunities for exploration and investigation. These activities incorporate concept and skill development and guided practice, then move on to the application of new skills and concepts in problem-solving situations. Throughout the lessons and activities, problems are contextualized to enhance rigor and relevance.

#### Introduction to the Program

This program includes all the topics addressed in the CCSS Traditional Pathway: Geometry content map. These include:

- Congruence, Proof, and Constructions
- Similarity, Proof, and Trigonometry
- Extending to Three Dimensions
- Connecting Algebra and Geometry Through Coordinates
- Circles With and Without Coordinates
- Applications of Probability

The eight Mathematical Practices described in the Common Core are infused throughout and are as follows:

- CCSS.MP.1: Make sense of problems and persevere in solving them.
- CCSS.MP.2: Reason abstractly and quantitatively.
- CCSS.MP.3: Construct viable arguments and critique the reasoning of others.
- CCSS.MP.4: Model with mathematics.
- CCSS.MP.5: Use appropriate tools strategically.
- CCSS.MP.6: Attend to precision.
- CCSS.MP.7: Look for and make use of structure.
- CCSS.MP.8: Look for and express regularity in repeated reasoning.

#### Structure of the Teacher Resource

The CCSS Traditional Pathway: Geometry Program is provided as a collection of unit books and an overview book, or in binder format. The materials are completely reproducible. You may also have purchased the CCSS Traditional Pathway: Geometry Teacher Resource in digital format. In this case, electronic "bookmarks" allow you to access the sections quickly and easily. The digital format also facilitates printing and copying student pages.

The Program Overview is the first section. Written for you, this section helps you to navigate the materials, offers several graphic organizers and suggested strategies for their use, and shows how the lessons correlate to the Common Core State Standards and the CCSS Traditional Pathway: Geometry content map found in Appendix A of the Common Core State Standards.

The remaining materials focus on content, knowledge, and application of the units in the CCSS Traditional Pathway: Geometry curriculum: Congruence, Proof, and Constructions; Similarity, Proof,

#### Introduction to the Program

and Trigonometry; Extending to Three Dimensions; Connecting Algebra and Geometry Through Coordinates; Circles With and Without Coordinates; and Applications of Probability. The units in the *CCSS Traditional Pathway: Geometry Program* are designed to be flexible so that you can mix and match activities as the needs of your students and your instructional style dictate.

The Station Activities correspond to the content in the units and provide students with the opportunity to apply concepts and skills, while you have a chance to circulate, observe, speak to individuals and small groups, and informally assess and plan.

Each lesson begins with a pre-assessment and ends with a progress assessment. These allow you to assess students' progress as you move from lesson to lesson, enabling you to gauge how well students have understood the material and to differentiate as appropriate.

#### Glossary

The Glossary contains vocabulary terms and formulas from throughout the program, organized alphabetically. Each listing provides the term and the definition in both English and Spanish.

## **Unit Structure**

All of the instructional units have common features. Each unit begins with a list of all the standards addressed in the topics and a list of one or more conceptual activities. Each unit also begins with a pre-assessment. Each topic begins with an overview of the standards addressed in the topic; Essential Questions; vocabulary (titled "Words to Know"); and a list of recommended websites to be used as additional resources.

Each lesson begins with a list of identified prerequisite skills that students need to have mastered in order to be successful with the new material in the upcoming lesson. This is followed by an introduction, key concepts, common errors/misconceptions, scaffolded practice problems, guided practice examples, a problem-based task with coaching questions and sample responses, a closure activity, and practice. Each topic ends with a progress assessment to evaluate students' learning.

All of the components are described below and on the following pages for your reference.

#### **Pre-Assessment**

This can be used to gauge students' prior knowledge and to inform instructional planning.

#### **Common Core State Standards for the Topic**

All standards that are addressed in the entire topic are listed.

#### **Essential Questions**

These are intended to guide students' thinking as they proceed through the topic. By the end of each topic, students should be able to respond to the questions.

#### **Words to Know**

Vocabulary terms and formulas are provided as background information for instruction or to review key concepts that are addressed in the topic.

#### **Recommended Resources**

This is a list of websites that can be used as additional resources. Some websites are games; others provide additional examples and/or explanations. (*Note*: Links will be monitored and repaired or replaced as necessary.) Each Recommended Resource is also accessible through Walch's cloud-based Curriculum Engine Learning Object Repository as a separate learning object that can be assigned to students.

#### **Unit Structure**

#### **Conceptual Activities**

Conceptual understanding serves as the foundation on which to build deeper understanding of mathematics. In an effort to build conceptual understanding of mathematical ideas and to provide more than procedural fluency and application, links to interactive open education and Desmos resources are included. (*Note*: These website links will be monitored and repaired or replaced as necessary.) These and many other open educational resources (OERs) are also accessible through the Learning Object Repository as separate objects that can be assigned to students.

#### Warm-Up

Each warm-up takes approximately 5 minutes and addresses either prerequisite and critical-thinking skills or previously taught math concepts.

#### **Common Core State Standards for the Lesson**

When topics are broken down into lessons, the specific standard or standards that are addressed are presented at the beginning of the instructional portion of the lesson.

#### Warm-Up Debrief

Each debrief provides the answers to the warm-up questions, and offers suggestions for situations in which students might have difficulties. A section titled Connection to the Lesson is also included in the debrief to help answer students' questions about the relevance of the particular warm-up activity to the upcoming instruction. Warm-Ups with debriefs are also provided in PowerPoint presentations.

#### **Identified Prerequisite Skills**

This list cites the skills necessary to be successful with the new material.

#### Introduction

This brief paragraph gives a description of the concepts about to be presented and often contains some Words to Know.

#### **Key Concepts**

Provided in bulleted form, this instruction highlights the important ideas and/or processes for meeting the standard.

#### **Graphing Calculator Directions**

Step-by-step instructions for using a TI-Nspire and a TI-83/84 are provided whenever graphing calculators are referenced.

#### **Unit Structure**

#### **Common Errors/Misconceptions**

This is a list of the common errors students make when applying Key Concepts. This list suggests what to watch for when students arrive at an incorrect answer or are struggling with solving the problems.

#### **Scaffolded Practice (Printable Practice)**

This set of 10 printable practice problems provides introductory level skill practice for the lesson. This practice set can be used during instruction time.

#### **Guided Practice**

This section provides step-by-step examples of applying the Key Concepts. The three to five examples are intended to aid during initial instruction, but are also for individuals needing additional instruction and/or for use during review and test preparation.

#### **Enhanced Instructional PowerPoint (Presentation)**

Each lesson includes an instructional PowerPoint presentation with the following components: Warm-Up, Key Concepts, and Guided Practice. Selected Guided Practice examples include GeoGebra applets. These instructional PowerPoints are downloadable and editable.

#### **Problem-Based Task**

This activity can serve as the centerpiece of a problem-based lesson, or it can be used to walk students through the application of the standard, prior to traditional instruction or at the end of instruction. The task makes use of critical-thinking skills.

#### **Optional Problem-Based Task Coaching Questions with Sample Responses**

These questions scaffold the task and guide students to solving the problem(s) presented in the task. They should be used at the discretion of the teacher for students requiring additional support. The Coaching Questions are followed by answers and suggested appropriate responses to the coaching questions. In some cases answers may vary, but a sample answer is given for each question.

#### **Recommended Closure Activity**

Students are given the opportunity to synthesize and reflect on the lesson through a journal entry or discussion of one or more of the Essential Questions.

#### **Unit Structure**

#### **Problem-Based Task Implementation Guide**

This instructional overview, found with selected Problem-Based Tasks in each unit, highlights connections between the task and the lesson's key concepts and Mathematical Practices. The Implementation Guide also offers suggestions for facilitating and monitoring, and provides alternative solutions.

#### Printable Practice (Sets A and B) and Interactive Practice (Set A)

Each lesson includes two sets of practice problems to support students' achievement of the learning objectives. They can be used in any combination of teacher-led instruction, cooperative learning, or independent application of knowledge. Each Practice A is also available as an interactive Learnosity activity with Technology-Enhanced Items.

#### **Progress Assessment**

Each lesson ends with 10 multiple-choice questions, as well as one extended-response question that incorporates critical thinking and writing components. This can be used to document the extent to which students grasp the concepts and skills addressed during instruction.

#### **Unit Assessment**

Each unit ends with 12 multiple-choice questions and three extended-response questions that incorporate critical thinking and writing components. This can be used to document the extent to which students grasped the concepts and skills of each unit.

#### **Answer Key**

Answers for all of the Warm-Ups and practice problems are provided at the end of each unit.

#### **Station Activities**

Most units include a collection of station-based activities to provide students with opportunities to practice, reinforce, and apply mathematical skills and concepts. The debriefing discussions after each set of activities provide an important opportunity to help students reflect on their experiences and synthesize their thinking.

#### **Conceptual Tasks**

These engaging tasks provide opportunities for students to deepen their understanding and develop their conceptual knowledge of math concepts. These tasks provide multiple entry points and are accessible for ALL learners.

## **Standards Correlations**

Each lesson in the *CCSS Geometry* program was written specifically to address the Common Core State Standards. Each lesson lists the standards covered in all the lessons, and each lesson lists the standards addressed in that particular section. In this section, you'll find a comprehensive list mapping the lessons to the CCSS.

#### **Guide to Common Core State Standards Annotation**

As you use this program, you will come across a symbol included with the Common Core standards for some of the lessons and activities. The description of the star symbol is found below, taken verbatim from the Common Core State Standards Initiative website, at <a href="https://www.corestandards.org">www.corestandards.org</a>.

#### Symbol: \*

#### **Denotes: Modeling Standards**

The Standards for Mathematical Practice describe varieties of expertise that mathematics educators at all levels should seek to develop in their students. These practices rest on important "processes and proficiencies" with longstanding importance in mathematics education. Specific modeling standards appear throughout the high school standards indicated by a star symbol (\*).

From http://www.walch.com/CCSS/00006

#### Symbol: (+)

#### **Denotes: College and Career Readiness Standards**

Advanced mathematics standards that are required in higher-level courses such as advanced statistics may also be included in lower-level courses. These additional standards are denoted by (+). According to the Common Core State Standards Initiative, "the evidence concerning college and career readiness shows clearly that the knowledge, skills, and practices important for readiness include a great deal of mathematics prior to the boundary defined by (+) symbols in these standards. Indeed, some of the highest priority content for college and career readiness comes from Grades 6–8."

From http://www.walch.com/CCSS/00004

#### **Connections to Future Courses**

This section provides a map between topics introduced in each unit of this course and subsequent courses where each topic is revisited and built upon.

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Topic	Lesson number	Title	Standard(s)			
	Unit 1: Congruence, Proof, and Constructions					
Topic A	Introducing Transformations					
	1.1	Defining Terms	G.CO.A.1			
	1.2	Transformations As Functions	G.CO.A.2			
	1.3	Applying Lines of Symmetry	G.CO.A.3			
Topic B	Rotations,	Reflections, and Translations				
	1.4	Defining Rotations, Reflections, and Translations	G.CO.A.4			
	1.5	Applying Rotations, Reflections, and Translations	G.CO.A.5			
Topic C	Exploring	Congruence				
	1.6	Describing Rigid Motions and Predicting the Effects	G.CO.B.6			
	1.7	Defining Congruence in Terms of Rigid Motions	G.CO.B.6			
Topic D	Congruent Triangles					
	1.8	Triangle Congruency	G.CO.B.7			
	1.9	Explaining ASA, SAS, SSS, AAS, and HL	G.CO.B.8			
Topic E	Proving Theorems About Lines and Angles					
	1.10	Proving the Vertical Angles Theorem	G.CO.C.9			
	1.11	Proving Theorems About Angles in Parallel Lines Cut by a Transversal	G.CO.C.9			
Topic F	Proving Theorems About Triangles					
	1.12	Proving the Interior Angle Sum Theorem	G.CO.C.10			
	1.13	Proving Theorems About Isosceles Triangles	G.CO.C.10			
	1.14	Proving the Midsegment of a Triangle	G.CO.C.10			
	1.15	Proving Centers of Triangles	G.CO.C.10			
Topic G	G Proving Theorems About Parallelograms					
	1.16	Proving Properties of Parallelograms	G.CO.C.11			
	1.17	Proving Properties of Special Quadrilaterals	G.CO.C.11			
Topic H	Constructing Lines, Segments, and Angles					
	1.18	Copying Segments and Angles	G.CO.D.12			
	1.19	Bisecting Segments and Angles	G.CO.D.12			
	1.20	Constructing Perpendicular and Parallel Lines	G.CO.D.12			

Topic	Lesson number	Title	Standard(s)		
Topic I	Constructing Polygons				
	1.21	Constructing Equilateral Triangles Inscribed in Circles	G.CO.D.13		
	1.22	Constructing Squares Inscribed in Circles	G.CO.D.13		
	1.23	Constructing Regular Hexagons Inscribed in Circles	G.CO.D.13		
		Unit 2: Similarity, Proof, and Trigonometry			
Topic A Investigating Properties of Dilations					
	2.1	Investigating Properties of Parallelism and the Center	G.SRT.A.1a		
	2.2	Investigating Scale Factors	G.SRT.A.1b		
Topic B	Defining a	nd Applying Similarity			
	2.3	Defining Similarity	G.SRT.A.2		
	2.4	Applying Similarity Using the Angle-Angle (AA) Criterion	G.SRT.A.3		
Topic C	<b>Proving Si</b>	milarity			
	2.5	Proving Triangle Similarity Using Side-Angle-Side (SAS) and Side-Side (SSS) Similarity	G.SRT.B.4		
	2.6	Working with Ratio Segments	G.SRT.B.4		
	2.7	Proving the Pythagorean Theorem Using Similarity	G.SRT.B.4		
	2.8	Solving Problems Using Similarity and Congruence	G.SRT.B.5		
Topic D	Exploring	Trigonometric Ratios			
	2.9	Defining Trigonometric Ratios	G.SRT.C.6		
	2.10	Exploring Sine and Cosine As Complements	G.SRT.C.7		
Topic E	Applying Trigonometric Ratios				
	2.11	Calculating Sine, Cosine, and Tangent	G.SRT.C.8 <sup>★</sup>		
	2.12	Calculating Cosecant, Secant, and Cotangent	G.SRT.C.8 <sup>★</sup>		
	2.13	Problem Solving with the Pythagorean Theorem and Trigonometry	G.SRT.C.8 <sup>★</sup>		
Topic F					
	2.14	Proving the Law of Sines	G.SRT.D.9 (+) G.SRT.D.10 (+)		
	2.15	Proving the Law of Cosines	G.SRT.D.10 (+)		
	2.16	Applying the Laws of Sines and Cosines	G.SRT.D.11 (+)		
Topic G	Trigonome	etric Modeling			
	2.17	Density	G.MG.A.2★		
	2.18	Design	G.MG.A.3★		

Topic	Lesson number	Title	Standard(s)		
		<b>Unit 3: Extending to Three Dimensions</b>			
Topic A	Explaining	g and Applying Area and Volume Formulas			
	3.1	Circumference and Area of a Circle	G.GMD.A.1		
	3.2	Volumes of Cylinders, Pyramids, Cones, and Spheres	G.GMD.A.1 G.GMD.A.3*		
Topic B	Two-Dime	nsional Cross Sections of Three-Dimensional Objects			
	3.3	Two-Dimensional Cross Sections of Three-Dimensional Objects	G.GMD.B.4 G.MG.A.1*		
	Unit 4:	Connecting Algebra and Geometry Through Coordinate	es		
Topic A	Slope and	Distance			
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	4.2	Working with Parallel and Perpendicular Lines	G.GPE.B.5		
Topic B	Points on Line Segments				
	4.3	Midpoints and Other Points on Line Segments	G.GPE.B.6		
Topic C	Calculating Perimeter and Area				
	4.4	Calculating Perimeter and Area	G.GPE.B.7★		
Topic D	Defining Parabolas Geometrically				
	4.5	Deriving the Equation of a Parabola	G.GPE.A.2		
	4.6	Using Coordinates to Prove Geometric Theorems About Parabolas	G.GPE.B.4		
		Unit 5: Circles With and Without Coordinates			
Topic A	Introducin	ng Circles			
	5.1	Similar Circles and Central and Inscribed Angles	G.C.A.1 G.C.A.2		
	5.2	Chord Central Angles Conjecture	G.C.A.2		
	5.3	Properties of Tangents of a Circle	G.C.A.2		
Topic B	Inscribed Polygons and Circumscribed Triangles				
	5.4	Constructing Inscribed Circles	G.C.A.3		
	5.5	Constructing Circumscribed Circles	G.C.A.3		
	5.6	Proving Properties of Inscribed Quadrilaterals	G.C.A.3		
Topic C	Constructi	ng Tangent Lines			
	5.7	Constructing Tangent Lines	G.C.A.4 (+)		

Topic	Lesson number	Title	Standard(s)	
Topic D	Finding Arc Lengths and Areas of Sectors			
	5.8	Defining Radians	G.C.B.5	
	5.9	Deriving the Formula for the Area of a Sector	G.C.B.5	
Topic E	The Equati	ion of a Circle		
	5.10	Deriving the Equation of a Circle	G.GPE.A.1	
	5.11	Using Coordinates to Prove Geometric Theorems About Circles	G.GPE.B.4	
Topic F	Geometric	Modeling with Circles		
	5.12	Modeling with Circles	G.MG.A.1	
		Unit 6: Applications of Probability		
Topic A	Events			
	6.1	Describing Events	S.CP.A.1★	
	6.2	The Addition Rule	S.CP.C.7*	
	6.3	Understanding Independent Events	S.CP.A.2★	
Topic B	Conditional Probability			
	6.4	Introducing Conditional Probability	S.CP.A.3★	
			S.CP.B.5*	
			S.CP.B.6*	
	6.5	Using Two-Way Frequency Tables	S.CP.A.4* S.CP.B.5*	
			S.CP.B.6*	
	6.6	The Multiplication Rule	S.CP.C.8* (+)	
Topic C				
1	6.7	Combinations and Permutations	S.CP.C.9* (+)	
	6.8	Probability with Combinatorics	S.CP.C.9* (+)	
Topic D	Making an	d Analyzing Decisions		
•	6.9	Making Decisions	S.MD.B.6* (+)	
	6.10	Analyzing Decisions	S.MD.B.7* (+)	