# North Carolina Math 3



**Program Overview** 



This program was developed and reviewed by experienced math educators who have both academic and professional backgrounds in mathematics. This ensures: freedom from mathematical errors, grade level appropriateness, freedom from bias, and freedom from unnecessary language complexity.

#### Developers and reviewers include:

| Jasmine Owens          | Tiffany Fele           | Jane Mando         |
|------------------------|------------------------|--------------------|
| Joanne Whitley         | Joseph Nicholson       | Timothy Trowbridge |
| Shelly Northrop Sommer | Jack Loynd             | Alan Hull          |
| Joyce Hale             | Terri Germain-Williams | Angela Heath       |
| Ruth Estabrook         | Laura McPartland       | Linda Kardamis     |
| Jacob Todd             | David Rawson           | Cameron Larkins    |
| Robert Leichner        | Lenore Horner          | Frederick Becker   |
| Michelle Adams         | Nancy Pierce           | Kimberly Brady     |
| Marie Vrablic          | Dale Blanchard         | Corey Donlan       |
| Kaithlyn Hollister     | Pamela Rawson          | Pablo Baques       |
| Carrisa Johnson-Scott  | Valerie Ackley         | Mike May, S.J.     |
| Samantha Carter        | Lynze Greathouse       | Whit Ford          |

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## Introduction to the Program

#### Introduction

The *North Carolina Math 3 Teacher Resource* is a complete set of materials developed around the North Carolina Standard Course of Study (NCSCOS) for Mathematics. Topics are built around accessible core curricula, ensuring that the *North Carolina Math 3 Teacher Resource* is useful for striving students and diverse classrooms.

This program realizes the benefits of exploratory and investigative learning and employs a variety of instructional models to meet the learning needs of students with a range of abilities.

The *North Carolina Math 3 Teacher Resource* includes components that support problem-based learning, instruct and coach as needed, provide practice, and assess students' skills. Instructional tools and strategies are embedded throughout.

#### The program includes:

- More than 150 hours of lessons
- Essential Questions for each instructional topic
- Vocabulary
- Instruction and Guided Practice
- Problem-based Tasks and Coaching questions
- Step-by-step graphing calculator instructions for the TI-Nspire and the TI-83/84
- Station activities to promote collaborative learning and problem-solving skills

#### **Purpose of Materials**

The *North Carolina Math 3 Teacher Resource* has been organized to coordinate with the North Carolina Math 3 content map and specifications from the NCSCOS. Each lesson includes activities that offer opportunities for exploration and investigation. These activities incorporate concept and skill development and guided practice, then move on to the application of new skills and concepts in problem-solving situations. Throughout the lessons and activities, problems are contextualized to enhance rigor and relevance.

#### Introduction to the Program

This program includes all the topics addressed in the North Carolina Math 3 content map. These include:

- Functions and Their Inverses
- Exponential and Logarithmic Functions
- Polynomial Functions
- Modeling with Geometry
- Reasoning with Geometry with Circles
- Rational Functions
- Trigonometric Functions
- Statistics

The eight Standards for Mathematical Practice are infused throughout:

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.

#### Structure of the Teacher Resource

The *North Carolina Math 3 Teacher Resource* materials are completely reproducible. The Program Overview is the first section. This section helps you to navigate the materials, offers a collection of research-based Instructional Strategies along with their literacy connections and implementation suggestions, and shows the correlation between the NCSCOS for Mathematics and the district-specfic content map and course requirements.

The remaining materials focus on content, knowledge, and application of the eight units in the North Carolina Math 3 program: Functions and Their Inverses, Exponential and Logarithmic Functions, Polynomial Functions, Modeling with Geometry, Reasoning with Geometry with Circles, Rational Functions, Trigonometric Functions, and Statistics. The units in this program are

#### Introduction to the Program

designed to be flexible so that you can mix and match activities as the needs of your students and your instructional style dictate.

The Station Activities correspond to the content in the units and provide students with the opportunity to apply concepts and skills, while you have a chance to circulate, observe, speak to individuals and small groups, and informally assess and plan.

Each unit includes a mid-unit assessment and an end-of-unit assessment. These enable you to gauge how well students have understood the material as you move from lesson to lesson and to differentiate as appropriate.

#### Glossary

The Glossary contains vocabulary terms and formulas from throughout the program, organized alphabetically by units. Each listing provides the term and the definition in both English and Spanish.

## **Unit Structure**

All of the instructional units have common features. Each unit begins with a list of all the standards addressed in the lessons; Essential Questions; vocabulary (titled "Words to Know"); a list of recommended websites to be used as additional resources, and one or more conceptual activities.

Each lesson begins with a warm-up, followed by a list of identified prerequisite skills that students need to have mastered in order to be successful with the new material in the upcoming lesson. This is followed by an introduction, key concepts, common errors/misconceptions, guided practice examples, a problem-based task with coaching questions and sample responses, a closure activity, and practice. Each unit includes a Mid-Unit Assessment and an End-of-Unit Assessment to evaluate students' learning.

All of the components are described below and on the following pages for your reference.

#### North Carolina Standard Course of Study for the Unit

All standards that are addressed in the entire unit are listed.

#### **Essential Questions**

These are intended to guide students' thinking as they proceed through the unit. By the end of each unit, students should be able to respond to the questions.

#### **Words to Know**

A list of vocabulary terms that appear in the unit are provided as background information for instruction or to review key concepts that are addressed in the lesson. Each term is followed by a numerical reference to the lesson(s) in which the term is defined.

#### **Recommended Resources**

This is a list of websites that can be used as additional resources. Some websites are games; others provide additional examples and/or explanations. (*Note*: Links will be monitored and repaired or replaced as necessary.) Each Recommended Resource is also accessible through Walch's cloud-based Curriculum Engine Learning Object Repository as a separate learning object that can be assigned to students.

#### **Conceptual Activities**

Conceptual understanding serves as the foundation on which to build deeper understanding of mathematics. In an effort to build conceptual understanding of mathematical ideas and to provide more than procedural fluency and application, links to interactive open education and Desmos resources are included. (*Note*: These website links will be monitored and repaired or replaced as necessary.) These and many other open educational resources (OERs) are also accessible through the Learning Object Repository as separate objects that can be assigned to students.

#### **Unit Structure**

#### Warm-Up

Each warm-up takes approximately 5 minutes and addresses either prerequisite and critical-thinking skills or previously taught math concepts.

#### Warm-Up Debrief

Each debrief provides the answers to the warm-up questions, and offers suggestions for situations in which students might have difficulties. A section titled Connection to the Lesson is also included in the debrief to help answer students' questions about the relevance of the particular warm-up activity to the upcoming instruction. Warm-Ups with debriefs are also provided in PowerPoint presentations.

#### **Identified Prerequisite Skills**

This list cites the skills necessary to be successful with the new material.

#### Introduction

This brief paragraph gives a description of the concepts about to be presented and often contains some Words to Know.

#### **Key Concepts**

Provided in bulleted form, this instruction highlights the important ideas and/or processes for meeting the standard.

#### **Graphing Calculator Directions**

Step-by-step instructions for using a TI-Nspire and a TI-83/84 are provided whenever graphing calculators are referenced.

#### **Common Errors/Misconceptions**

This is a list of the common errors students make when applying Key Concepts. This list suggests what to watch for when students arrive at an incorrect answer or are struggling with solving the problems.

#### **Scaffolded Practice (Printable Practice)**

This set of 10 printable practice problems provides introductory level skill practice for the lesson. This practice set can be used during instruction time.

#### **Unit Structure**

#### **Guided Practice**

This section provides step-by-step examples of applying the Key Concepts. The three to five examples are intended to aid during initial instruction, but are also for individuals needing additional instruction and/or for use during review and test preparation.

#### **Enhanced Instructional PowerPoint (Presentation)**

Each lesson includes an instructional PowerPoint presentation with the following components: Warm-Up, Key Concepts, and Guided Practice. Selected Guided Practice examples include GeoGebra applets. These instructional PowerPoints are downloadable and editable.

#### **Problem-Based Task**

This activity can serve as the centerpiece of a problem-based lesson, or it can be used to walk students through the application of the standard, prior to traditional instruction or at the end of instruction. The task makes use of critical-thinking skills.

#### **Optional Problem-Based Task Coaching Questions with Sample Responses**

These questions scaffold the task and guide students to solving the problem(s) presented in the task. They should be used at the discretion of the teacher for students requiring additional support. The Coaching Questions are followed by answers and suggested appropriate responses to the coaching questions. In some cases answers may vary, but a sample answer is given for each question.

#### **Recommended Closure Activity**

Students are given the opportunity to synthesize and reflect on the lesson through a journal entry or discussion of one or more of the Essential Questions.

#### **Problem-Based Task Implementation Guide**

This instructional overview, found with selected Problem-Based Tasks in each unit, highlights connections between the task and the lesson's key concepts and SMPs. The Implementation Guide also offers suggestions for facilitating and monitoring, and provides alternative solutions.

#### Printable Practice (Sets A and B) and Interactive Practice (Set A)

Each lesson includes two sets of practice problems to support students' achievement of the learning objectives. They can be used in any combination of teacher-led instruction, cooperative learning, or independent application of knowledge. Each Practice A is also available as an interactive Learnosity activity with Technology-Enhanced Items.

#### **Unit Structure**

#### **Answer Key**

Answers for all of the Warm-Ups and practice problems are provided at the end of each unit.

#### **Station Activities**

Each unit includes a collection of station-based activities to provide students with opportunities to practice, reinforce, and apply mathematical skills and concepts. The debriefing discussions after each set of activities provide an important opportunity to help students reflect on their experiences and synthesize their thinking.

#### **Conceptual Tasks**

These engaging tasks provide opportunities for students to deepen their understanding and develop their conceptual knowledge of math concepts. These tasks provide multiple entry points and are accessible for ALL learners.

#### Mid-Unit and End-of-Unit Assessments

A mid-unit assessment and an end-of-unit assessment offer multiple-choice questions and extended-response questions that incorporate critical thinking and writing components. These can be used to document the extent to which students grasped the concepts and skills of each unit.

## **Standards Correlations**

Each lesson in this program was written specifically to address the North Carolina Standard Course of Study (NCSCOS) for Mathematics. Each unit lists the standards covered in all the lessons, and each lesson lists the standards addressed in that particular lesson. In this section, you'll find a comprehensive list mapping the lessons to the NCSCOS.

As you use this program, you will come across a star symbol (\*) included with the standards for some of the lessons and activities. This symbol is explained below.

#### Symbol: \*

#### **Denotes: Modeling Standards**

Modeling is best interpreted not as a collection of isolated topics but rather in relation to other standards. Making mathematical models is a Standard for Mathematical Practice, and specific modeling standards appear throughout the high school standards indicated by a star symbol (\*).

From http://www.walch.com/CCSS/00003

|        | <b>Unit 1: Functions and Their Inverses</b>  |                                  |  |  |  |
|--------|--|----------------------------------|--|--|--|
| Lesson | Title  | Standard(s)                      |  |  |  |
| 1.1    | Comparing Properties of Functions Given in Different Forms                         | F–IF.9, F–LE.3                   |  |  |  |
| 1.2    | Graphing Radical Functions   | F–IF.7*                          |  |  |  |
| 1.3    | Creating Absolute Value Equations and Inequalities in One Variable                 | A-CED.1*                         |  |  |  |
| 1.4    | Absolute Value and Step Functions  | F–IF.7*                          |  |  |  |
| 1.5    | Creating and Graphing Absolute Value Equations and Inequalities with Two Variables | A-CED.2*, A-CED.3*,<br>A-REI.11* |  |  |  |
| 1.6    | Piecewise Functions  | F–IF.7*                          |  |  |  |
| 1.7    | Operating on Functions   | F-BF.1b*                         |  |  |  |
| 1.8    | Finding Inverse Functions  | F–BF.4a                          |  |  |  |
| 1.9    | Finding Inverse Functions in Various Forms   | F–BF.4c, F–IF.9                  |  |  |  |
| 1.10   | Determining Inverses of Quadratic Functions  | F–BF.4c                          |  |  |  |

| <b>Unit 2: Exponential and Logarithmic Functions</b> |   |                     |
|--|---|---------------------|
| Lesson   | <b>Lesson</b> Title   |                     |
| 2.1  | Creating and Interpreting Exponential Functions               | A-CED.1*, A-SSE.1a* |
| 2.2  | Translating Exponential Functions                             | F-BF.3              |
| 2.3  | Logarithmic Functions as Inverses                             | F-BF.4a, F-BF.4c    |
| 2.4  | Graphing Logarithmic Functions                                | F–LE.4*             |
| 2.5  | Solving Exponential Equations                                 | F–LE.4*             |
| 2.6  | Creating and Solving Exponential Equations from Word Problems | A-CED.1*            |
| 2.7  | Writing Exponential Expressions in Equivalent Forms           | A–SSE.3*            |
| 2.8  | Linear, Exponential, and Quadratic Functions                  | A–CED.2*, F–IF.9    |

|        | <b>Unit 3: Polynomial Functions</b>    |                 |  |
|--------|--|-----------------|--|
| Lesson | Title                                  | Standard(s)     |  |
| 3.1    | Introduction to Polynomial Functions   | A–SSE.1a*       |  |
| 3.2    | Graphing Quadratic and Cubic Functions | F-IF.7*         |  |
| 3.3    | Optimization of Volume                 | G-MG.1*         |  |
| 3.4    | Describing End Behavior and Turns      | F-IF.7*, N-CN.9 |  |
| 3.5    | The Remainder Theorem                  | A–APR.2         |  |
| 3.6    | Zeros of Polynomial Functions          | A–APR.3         |  |
| 3.7    | Building Polynomial Functions          | F-BF.1a*        |  |
| 3.8    | End Behaviors of Functions             | F-LE.3*, F-IF.9 |  |

| Unit 4: Modeling with Geometry |   |             |  |
|--------------------------------|---|-------------|--|
| Lesson                         | Title   | Standard(s) |  |
| 4.1                            | Proving Theorems About Triangles                            | G-CO.10     |  |
| 4.2                            | Proving Properties of Parallelograms                        | G-CO.11     |  |
| 4.3                            | Proving Properties of Special Quadrilaterals                | G-CO.11     |  |
| 4.4                            | Two-Dimensional Cross Sections of Three-Dimensional Objects | G-GMD.4     |  |
| 4.5                            | Volumes of Cylinders, Pyramids, Cones, and Spheres          | G-GMD.3*    |  |
| 4.6                            | Density   | G-MG.1*     |  |
| 4.7                            | Design  | G-MG.1*     |  |
| 4.8                            | Proving Centers of Triangles                                | G-CO.10     |  |

| Unit 5: Reasoning with Geometry with Circles |  |                  |  |
|--|--|------------------|--|
| Lesson                                       | Title  | Standard(s)      |  |
| 5.1  | Deriving the Equation of a Circle                | G-GPE.1, G-CO.14 |  |
| 5.2  | Similar Circles and Central and Inscribed Angles | G-C.2            |  |
| 5.3  | Chord Central Angles Conjecture                  | G-C.2            |  |
| 5.4  | Defining Radians                                 | G-C.5            |  |
| 5.5  | Deriving the Formula for the Area of a Sector    | G-C.5            |  |
| 5.6  | Properties of Tangents of a Circle               | G-C.2, G-CO.14   |  |
| 5.7  | Inscribed Angles, Secants, Tangents, and Chords  | G-C.2            |  |

| <b>Unit 6: Rational Functions</b> |  |                                |  |
|-----------------------------------|--|--------------------------------|--|
| Lesson                            | Title  | Standard(s)                    |  |
| 6.1                               | Graphing Rational Equations                              | A-CED.2*                       |  |
| 6.2                               | Graphing Rational Functions and Identifying Key Features | A–SSE.1a*, F–IF.4*,<br>F–IF.7* |  |
| 6.3                               | Structures of Rational Expressions                       | A–APR.6                        |  |
| 6.4                               | Multiplying Rational Expressions                         | A–APR.7b                       |  |
| 6.5                               | Dividing Rational Expressions                            | A–APR.7b                       |  |
| 6.6                               | Adding and Subtracting Rational Expressions              | A–SSE.2, A–APR.7a              |  |
| 6.7                               | Solving Rational Equations                               | A–REI.2                        |  |
| 6.8                               | Creating Rational Equations                              | A-CED.1*                       |  |

| Unit 7: Trigonometric Functions |   |                |  |
|---------------------------------|---|----------------|--|
| Lesson                          | Title   | Standard(s)    |  |
| 7.1                             | Radians   | F–IF.1, F–TF.1 |  |
| 7.2                             | Special Angles in the Unit Circle                           | F-TF.2         |  |
| 7.3                             | Periodic Phenomena and Amplitude, Frequency, and<br>Midline | F-TF.5*        |  |
| 7.4                             | Using Trigonometric Functions to Model Periodic Phenomena   | F-TF.5*        |  |

| Unit 8: Statistics |  |             |  |
|--------------------|--|-------------|--|
| Lesson             | Title  | Standard(s) |  |
| 8.1                | Identifying Surveys, Experiments, and<br>Observational Studies | S–IC.3*     |  |
| 8.2                | Other Methods of Random Sampling                               | S-IC.3*     |  |
| 8.3                | Differences Between Populations and Samples                    | S-IC.3*     |  |
| 8.4                | Designing Surveys, Experiments, and Observational Studies      | S–IC.3*     |  |
| 8.5                | Designing and Simulating Treatments                            | S–IC.5*     |  |
| 8.6                | Estimating Sample Proportions                                  | S-IC.4*     |  |
| 8.7                | Estimating Sample Means  | S-IC.4*     |  |
| 8.8                | Reading Reports  | S–IC.6*     |  |