

Texas Essential Knowledge and Skills

Mathematical Models with Applications



Program Overview

This program was developed and reviewed by experienced math educators who have both academic and professional backgrounds in mathematics. This ensures: freedom from mathematical errors, grade level appropriateness, freedom from bias, and freedom from unnecessary language complexity.

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Introduction to the Program

Introduction

The *TEKS Mathematical Models with Applications Program* is a complete set of materials developed to be aligned to the Texas Essential Knowledge and Skills (TEKS) and the Mathematical Models with Applications content map. Topics are built around accessible core curricula, ensuring that the *TEKS Mathematical Models with Applications Program* is useful for college-ready students and diverse classrooms.

This program realizes the benefits of exploratory and investigative learning and employs a variety of instructional models to meet the learning needs of students with a range of abilities.

The *TEKS Mathematical Models with Applications Program* includes components that support problem-based learning, instruct and coach as needed, provide practice, and assess students' skills. Instructional tools and strategies are embedded throughout.

The program includes:

- More than 165 hours of lessons
- Essential Questions for each instructional topic
- Vocabulary
- Instruction and Guided Practice
- Sets of standards-based Scaffolded Practice and Practice problems
- Problem-based Tasks and Coaching questions
- Step-by-step graphing calculator instructions for the TI-Nspire and the TI-83/84
- Performance Tasks to promote collaborative learning and problem-solving skills
- Aligned open education resources that enhance procedural fluency and conceptual understanding
- Embedded Instructional Strategies to enable access for all students

Purpose of Materials

The *TEKS Mathematical Models with Applications Program* has been organized to coordinate with the TEKS Mathematical Models with Applications content map and specifications from the Texas Essential Knowledge and Skills.

Each topic includes activities that offer opportunities for exploration and investigation. These activities incorporate concept and skill development and guided practice, then move on to the application of new skills and concepts in problem-solving situations. Throughout the lessons and

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Introduction to the Program

activities, problems are contextualized to enhance rigor and relevance.

This program includes all the topics addressed in the TEKS Mathematical Models with Applications content map. These include:

- Data Collection and Analysis
- Mathematical Models in Research
- Mathematical Models in Science and Engineering
- Probability
- Personal Finance: Income, Taxes, and Budgeting
- Personal Finance: Savings and Investment
- Personal Finance: Credit, Loans, and Insurance
- Mathematical Models in Architecture and Spatial Reasoning
- Mathematical Models in the Fine Arts

The Mathematical Process Standards described in the Texas Essential Knowledge and Skills are infused throughout. The student is expected to:

- (A) apply mathematics to problems arising in everyday life, society, and the workplace;
- (B) use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the problem-solving process and the reasonableness of the solution;
- (C) select tools, including real objects, manipulatives, paper and pencil, and technology as appropriate, and techniques, including mental math, estimation, and number sense as appropriate, to solve problems;
- (D) communicate mathematical ideas, reasoning, and their implications using multiple representations, including symbols, diagrams, graphs, and language as appropriate;
- (E) create and use representations to organize, record, and communicate mathematical ideas;
- (F) analyze mathematical relationships to connect and communicate mathematical ideas; and
- (G) display, explain, and justify mathematical ideas and arguments using precise mathematical language in written or oral communication.

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Introduction to the Program

Structure of the Teacher Resource

The *TEKS Mathematical Models with Applications Teacher Resource* materials are completely reproducible. The Program Overview is the first section. This section helps you to navigate the materials, offers a collection of research-based Instructional Strategies along with their literacy connections and implementation suggestions, and shows the correlation between the Texas Essential Knowledge and Skills and the Mathematical Models with Applications content map and course requirements.

The remaining materials focus on building math content knowledge and conceptual understanding through application of the units in the *Mathematical Models with Applications* program: Data Collection and Analysis; Mathematical Models in Research; Mathematical Models in Science and Engineering; Probability; Personal Finance: Income, Taxes, and Budgeting; Personal Finance: Savings and Investment; Personal Finance: Credit, Loans, and Insurance; Mathematical Models in Architecture and Spatial Reasoning; and Mathematical Models in the Fine Arts. The units in the *TEKS Mathematical Models with Applications Program* are designed to be flexible so that you can mix and match activities as the needs of your students and your instructional style dictate.

The Performance Tasks correspond to the content in selected units and provide students with the opportunity to apply concepts and skills, while you have a chance to circulate, observe, speak to individuals and small groups, and informally assess and plan.

Each unit includes a pre-assessment and unit assessment, and each topic ends with a progress assessment. These allow you to assess students' progress as you move from topic to topic, enabling you to gauge how well students have understood the material and to differentiate as appropriate.

Glossary

The Glossary contains vocabulary terms and formulas from throughout the program, organized alphabetically by units. Each listing provides the term and the definition in both English and Spanish.

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Unit Structure

All of the instructional units have common features. Each unit begins with a list of all the standards addressed in the topics and a list of one or more conceptual activities. Each unit also begins with a pre-assessment. Each topic begins with an overview of the standards addressed in the topic; Essential Questions; vocabulary (titled “Words to Know”); and a list of recommended websites to be used as additional resources.

Each lesson begins with a list of identified prerequisite skills that students need to have mastered in order to be successful with the new material in the upcoming lesson. This is followed by an introduction, key concepts, common errors/misconceptions, scaffolded practice problems, guided practice examples, a problem-based task with coaching questions and sample responses, a closure activity, and practice. Each topic ends with a progress assessment to evaluate students’ learning.

All of the components are described below and on the following pages for your reference.

Standards Correlations

In this section, you’ll find a comprehensive list of the Texas Essential Knowledge and Skills addressed in each lesson.

Conceptual Activities

Conceptual understanding serves as the foundation on which to build deeper understanding of mathematics. In an effort to build conceptual understanding of mathematical ideas and to provide more than procedural fluency and application, links to interactive open education and Desmos resources are included. (*Note:* These website links will be monitored and repaired or replaced as necessary.) These and many other open educational resources (OERs) are also accessible through the Learning Object Repository as separate objects that can be assigned to students.

Unit Pre-Assessment and Answer Key with TEKS

This can be used to gauge students’ prior knowledge and to inform instructional planning. The assessment is followed by an answer key that lists the Texas Essential Knowledge and Skills addressed by each problem.

Instructional Strategies

These research-based strategies are intended to provide additional support for teachers using Walch’s resources. Implementation guides for these instructional strategies can be found later in the program overview, while icons are located throughout the instructional resources to indicate appropriate strategies at the point of use. Inclusion of these strategies along with additional resources for English as a Second Language (ESL) students, SWD students, and struggling readers will provide teachers with a wide range of instructional support.

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Unit Structure

Texas Essential Knowledge and Skills for the Topic

All standards that are addressed in the entire topic are listed.

Essential Questions

These are intended to guide students' thinking as they proceed through the lesson. By the end of each lesson, students should be able to respond to the questions.

Words to Know

A list of vocabulary terms that appear in the unit are provided as background information for instruction or to review key concepts that are addressed in the lesson. Each term is followed by a numerical reference to the first lesson in which the term is defined.

Recommended Resources

This is a list of websites that can be used as additional resources. Some websites are games; others provide additional examples and/or explanations. The links for these resources are live in the PDF version of the Teacher Resource. (*Note:* These website links will be monitored and repaired or replaced as necessary.) Each Recommended Resource is also accessible through Walch's cloud-based Curriculum Engine Learning Object Repository as a separate learning object that can be assigned to students.

Warm-Up

Each warm-up takes approximately 5 minutes and addresses either prerequisite and critical-thinking skills or previously taught math concepts.

Warm-Up Debrief

Each debrief provides the answers to the warm-up questions, and offers suggestions for situations in which students might have difficulties. A section titled Connection to the Lesson is also included in the debrief to help answer students' questions about the relevance of the particular warm-up activity to the upcoming instruction. Warm-Ups with debriefs are also provided in PowerPoint presentations.

Identified Prerequisite Skills

This list cites the skills necessary to be successful with the new material.

Introduction

This brief section gives a description of the concepts about to be presented and often contains some Words to Know.

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Unit Structure

Key Concepts

Provided in bulleted form, this instruction highlights the important ideas and/or processes for meeting the standard.

Graphing Calculator Directions

Step-by-step instructions for using a TI-Nspire and a TI-83/84 are provided whenever graphing calculators are referenced.

Common Errors/Misconceptions

This is a list of the common errors students make when applying Key Concepts. The list suggests what to watch for when students arrive at an incorrect answer or are struggling with solving the problems.

Scaffolded Practice (Printable Practice)

This set of 10 printable practice problems provides introductory level skill practice for the lesson. This practice set can be used during instruction time.

Guided Practice

This section provides step-by-step examples of applying the Key Concepts. The three to five examples are intended to aid during initial instruction, but are also for individuals needing additional instruction and/or for use during review and test preparation.

Enhanced Instructional PowerPoint (Presentation)

Each lesson includes an instructional PowerPoint presentation with the following components: Warm-Up, Key Concepts, and Guided Practice. Selected Guided Practice examples include GeoGebra applets. These instructional PowerPoints are downloadable and editable.

Problem-Based Task

This activity can serve as the centerpiece of a problem-based lesson, or it can be used to walk students through the application of the standard, prior to traditional instruction or at the end of instruction. The task makes use of critical-thinking skills.

Optional Problem-Based Task Coaching Questions with Sample Responses

These questions scaffold the task and guide students to solving the problem(s) presented in the task. They should be used at the discretion of the teacher for students requiring additional support. The Coaching Questions are followed by answers and suggested appropriate responses to the coaching questions. In some cases answers may vary, but a sample answer is given for each question.

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Unit Structure

Recommended Closure Activity

Students are given the opportunity to synthesize and reflect on the lesson through a journal entry or discussion of one or more of the Essential Questions.

Printable Practice (Sets A and B) and Interactive Practice (Set A)

Each lesson includes two sets of practice problems to support students' achievement of the learning objectives. They can be used in any combination of teacher-led instruction, cooperative learning, or independent application of knowledge. Each Practice A is also available as an interactive Learnosity activity with Technology-Enhanced Items.

Conceptual Tasks

These engaging tasks provide opportunities for students to deepen their understanding and develop their conceptual knowledge of math concepts. These tasks provide multiple entry points and are accessible for ALL learners.

Topic Progress Assessment and Answer Key with TEKS

Each topic ends with 10 multiple-choice questions, as well as one extended-response question that incorporates critical thinking and writing components. This can be used to document the extent to which students grasp the concepts and skills addressed during instruction. The answer key that follows correlates each problem to the targeted Standard(s).

Answer Key

Answers for all of the Warm-Ups and practice problems are provided following each unit.

Unit Assessment and Answer Key with TEKS

Each unit ends with 12 multiple-choice questions and three extended-response questions that incorporate critical thinking and writing components. This can be used to document the extent to which students grasped the concepts and skills of each unit. Targeted TEKS are listed in the answer key.

Performance Task

Selected units include an extension activity to provide students with opportunities to practice, reinforce, and apply mathematical skills and concepts to a real-world task.

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Standards Correlations

Each topic in this TEKS Mathematical Models with Applications program was written specifically to address the Texas Essential Knowledge and Skills (TEKS). Each topic lists the standards covered in all the lessons, and each lesson lists the standards addressed in that particular lesson. In this section, you'll find a comprehensive list mapping the lessons to the TEKS.

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Standards Correlations

Unit 1: Data Collection and Analysis			
Topic	Lesson number	Title	Standard(s)
Topic A	Summarizing, Representing, and Interpreting Data		
	1.1	Data Types and Visualizations	TEKS.MMA.9A
	1.2	Comparing Different Data Sets	TEKS.MMA.9A, TEKS.MMA.9B
	1.3	Interpreting Data and Recognizing Outliers	TEKS.MMA.9A, TEKS.MMA.9B
Topic B	The Normal Curve		
	1.4	The Normal Curve	TEKS.MMA.9B
Topic C	Identifying Surveys, Experiments, and Observational Studies		
	1.5	Identifying Surveys, Experiments, and Observational Studies	TEKS.MMA.9C

Unit 2: Mathematical Models in Research			
Topic	Lesson number	Title	Standard(s)
Topic A	Populations Versus Random Samples, Random Sampling, and Bias		
	2.1	Differences Between Populations and Samples	TEKS.MMA.9D
	2.2	Simple Random Sampling	TEKS.MMA.9D
	2.3	Sampling Methods and Sources of Bias	TEKS.MMA.9D
Topic B	Evaluating the Significance of Sample Statistics		
	2.4	Confidence in Sample Statistics	TEKS.MMA.9D
	2.5	Estimating with Confidence	TEKS.MMA.9D, TEKS.MMA.9E
	2.6	Reading Reports	TEKS.MMA.9E
Topic C	Line of Best Fit		
	2.7	Solving Problems Given Functions Fitted to Data	TEKS.MMA.9F
	2.8	Analyzing Residuals	TEKS.MMA.9F
	2.9	Fitting Linear Functions to Data	TEKS.MMA.9F
	2.10	Fitting Exponential Functions to Data	TEKS.MMA.9F
Topic D	Interpreting Statistical Models		
	2.11	Interpreting Fitted Functions	TEKS.MMA.9F
	2.12	Calculating and Interpreting the Correlation Coefficient	TEKS.MMA.9F
	2.13	Distinguishing Between Correlation and Causation	TEKS.MMA.9F

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Unit 3: Mathematical Models in Science and Engineering			
Topic	Lesson number	Title	Standard(s)
Topic A	Direct and Inverse Variations		
	3.1	Ramp-Up Lesson: Rearranging Formulas	TEKS.MMA.5A
	3.2	Direct and Inverse Variation	TEKS.MMA.5A
Topic B	Ramp-Up Topic: Interpreting Exponential Graphs		
	3.3	Ramp-Up Lesson: Identifying Key Features of Exponential Graphs	TEKS.A1.9B, TEKS.A1.9D
Topic C	Modeling with Exponential Equations		
	3.4	Exponential Regression in Science	TEKS.MMA.5B, TEKS.MMA.5F
	3.5	Exponential Functions as Models	TEKS.MMA.5B
Topic D	Ramp-Up Topic: Interpreting Structure in Expressions		
	3.6	Ramp-Up Lesson: Identifying Terms, Factors, and Coefficients	TEKS.6.7B
	3.7	Ramp-Up Lesson: Interpreting Complicated Expressions	TEKS.A1.7B
Topic E	Ramp-Up Topic: Factoring		
	3.8	Ramp-Up Lesson: Factoring Expressions by the Greatest Common Factor	TEKS.A1.10E
	3.9	Ramp-Up Lesson: Factoring Expressions with $a = 1$	TEKS.A1.10E
	3.10	Ramp-Up Lesson: Factoring Expressions with $a > 1$	TEKS.A1.10E
Topic F	Modeling with Quadratics		
	3.11	Converting Quadratic Equations to Different Forms	TEKS.MMA.5C
	3.12	Building Quadratic Equations from Context	TEKS.MMA.5C

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Unit 4: Probability			
Topic	Lesson number	Title	Standard(s)
Topic A	Representing Sample Spaces and Events		
	4.1	Drawing and Interpreting Venn and Tree Diagrams	TEKS.MMA.8A, TEKS.MMA.9A
	4.2	Identifying Sample Spaces	TEKS.MMA.8A, TEKS.MMA.9A
	4.3	Identifying Events	TEKS.MMA.8A, TEKS.MMA.9A
	4.4	Describing Events	TEKS.MMA.8A, TEKS.MMA.9A
	4.5	Combinations and Permutations	TEKS.MMA.8A
Topic B	Calculating Probabilities		
	4.6	Calculating Probabilities and Expressing them in Equivalent Forms Using Fractions, Decimals, and Percents	TEKS.MMA.8A
	4.7	Probability with Combinatorics	TEKS.MMA.8A
Topic C	Theoretical and Empirical Probability		
	4.8	Comparing Theoretical to Empirical Probability	TEKS.MMA.8B
	4.9	Assessing Theoretical Probability Models	TEKS.MMA.8C

Unit 5: Personal Finance: Income, Taxes, and Budgeting			
Topic	Lesson number	Title	Standard(s)
Topic A	Income		
	5.1	Creating Equations and Inequalities—Gross Pay	TEKS.MMA.2A
	5.2	Creating Equations in Context—Net Pay	TEKS.MMA.2A
Topic B	Taxation		
	5.3	Creating and Solving Equations in Two Variables—Tax Brackets	TEKS.MMA.2B
Topic C	Budgeting		
	5.4	Functions, Systems and Budgets	TEKS.MMA.2A

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Unit 6: Personal Finance: Credit, Loans, and Insurance			
Topic	Sub-lesson number	Title	Standard(s)
Topic A	Credit		
	6.1	Solving Linear Equations—Simple Interest	TEKS.MMA.3B
	6.2	Analyzing Credit Offers with Linear and Exponential Equations	TEKS.MMA.3B
Topic B	Loans and Financed Purchases		
	6.3	Recursion and Sequences—Payment Plans	TEKS.MMA.3A, TEKS.MMA.3C, TEKS.MMA.3D
	6.4	Finite Geometric Series—Amortized Loans	TEKS.MMA.3A, TEKS.MMA.3C, TEKS.MMA.3D
Topic C	Insurance		
	6.5	Insurance	TEKS.MMA.4A

Unit 7: Personal Finance: Savings and Investment			
Topic	Lesson number	Title	Standard(s)
Topic A	Banking		
	7.1	Interpreting Complicated Expressions—Bank Statements and Savings Accounts	TEKS.MMA.2C, TEKS.MMA.4C
	7.2	Creating Equations and Inequalities—Savings Interest	TEKS.MMA.2C, TEKS.MMA.4C
Topic B	Investing		
	7.3	Interpreting Expressions and Equations—Stocks and Shares	TEKS.MMA.4B
	7.4	Interpreting Stock Parameters	TEKS.MMA.4B
	7.5	Reading Stock Reports	TEKS.MMA.4B
Topic C	Planning for Retirement		
	7.6	Planning for Retirement	TEKS.MMA.4B

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Unit 8: Mathematical Models in Architecture and Spatial Reasoning			
Topic	Sub-lesson number	Title	Standard(s)
Topic A	Ramp-Up: Investigating Properties of Dilations		
	8.1	Ramp-up: Dilations and Parallel Lines	TEKS.G.3B
	8.2	Ramp-up: Finding and Using Scale Factors	TEKS.G.3B
Topic B	Ramp-Up: Defining and Applying Similarity		
	8.3	Ramp-up: Defining Similarity	TEKS.G.7A
	8.4	Ramp-up: Applying Similarity Using the Angle-Angle (AA) Criterion	TEKS.G.7B
Topic C	Ramp-Up: Proving Similarity		
	8.5	Ramp-up: Side-Angle-Side (SAS) and Side-Side-Side (SSS) Similarity	TEKS.G.8A
	8.6	Ramp-up: Ratios and Similarity	TEKS.G.8A
	8.7	Ramp-up: The Pythagorean Theorem and Similarity	TEKS.G.6D, TEKS.G.8A
	8.8	Ramp-up: Solving Problems Using Similarity and Congruence	TEKS.G.6D, TEKS.G.8A
Topic D	Ramp-up: 45°–45°–90° and 30°–60°–90° Triangles		
	8.9		TEKS.G.9B
	Topic D Exploring and Applying Trigonometric Ratios		
	8.10	Defining Sine, Cosine, and Tangent	TEKS.MMA.6D
	8.11	Calculating Sine, Cosine, and Tangent	TEKS.MMA.6D
Topic E	Problem Solving with the Pythagorean Theorem and Trigonometry		
	8.12		TEKS.MMA.6D, TEKS.MMA.6C
	Topic E Creating and Using Geometric Models		
	8.13	Scaling Across Dimensions	TEKS.MMA.6B, TEKS.MMA.7D
	8.14	Modeling in Three Dimensions	TEKS.MMA.6A, TEKS.MMA.6B, TEKS.MMA.6C, TEKS.MMA.6D

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Unit 9: Mathematical Models in the Fine Arts			
Topic	Sub-lesson number	Title	Standard(s)
Topic A	Introducing Trigonometric Functions		
	9.1	Ramp-Up Lesson: Radians	TEKS.G.12D
	9.2	Ramp-Up Lesson: The Unit Circle	TEKS.G.12D
	9.3	Ramp-Up Lesson: Special Angles in the Unit Circle	TEKS.G.12D
	9.4	Ramp-Up Lesson: Evaluating Trigonometric Functions	TEKS.G.9A
Topic B	Trigonometric Functions in Art and Music		
	9.5	Periodic Phenomena and Amplitude, Frequency, and Midline	TEKS.MMA.7A, TEKS.MMA.7C
	9.6	Using Trigonometric Functions to Model Periodic Phenomena	TEKS.MMA.7A, TEKS.MMA.7C
Topic C	Math in Music		
	9.7	Patterns and Symmetry in Music	TEKS.MMA.7C
	9.8	Applying Mathematics to Music	TEKS.MMA.7A, TEKS.MMA.7C
Topic D	Scale and Dimension in Art		
	9.9	Proportions and Perspective	TEKS.MMA.7B
	9.10	Dimension in Art	TEKS.MMA.7B, TEKS.MMA.7D